

The role of temperature dependence of ion-ion reactions in determining the mechanism

Reaction:  $A + B \rightleftharpoons AB^\ddagger \rightarrow \text{products}$

Based on the relations  $\Delta S = -\left(\frac{\partial \Delta G}{\partial T}\right)_P$  and  $\Delta G_{e.s.} = \frac{Nz_A z_B e^2}{4\pi\epsilon_0\epsilon_r r_\ddagger}$ , we have

$$\Delta S_{e.s.}^\ddagger = \frac{Nz_A z_B e^2}{4\pi\epsilon_0\epsilon_r^2 r_\ddagger} \left(\frac{\partial \epsilon_r}{\partial T}\right)_P = \frac{Nz_A z_B e^2}{4\pi\epsilon_0\epsilon_r r_\ddagger} \left(\frac{\partial \ln \epsilon_r}{\partial T}\right)_P$$

With  $N = 6.022 \times 10^{23} \text{ mol}^{-1}$ ,  $e = 1.602 \times 10^{-19} \text{ C}$  and  $\epsilon_0 = 8.854 \times 10^{-12} \text{ F/m}$  (or  $\text{C}/(\text{Vm})$ ), using typical data in a solvent of water:  $\epsilon_0 \approx 80$ ,  $r_\ddagger = 200 \text{ pm}$  and  $\left(\frac{\partial \ln \epsilon_r}{\partial T}\right)_P \approx -0.0046 \text{ K}^{-1}$ , we get

$$\Delta S_{e.s.}^\ddagger \approx -40z_A z_B \frac{\text{J}}{\text{mol K}}$$

As the pre-exponential factor in the Arrhenius equation is  $A = \frac{k_B T}{h} e^{\frac{\Delta S^\ddagger}{R}}$ , we get

$$\Delta S_{e.s.}^\ddagger \approx -4.8 z_A z_B$$

Thus

$$e^{-4.8 z_A z_B} = 10^{-\frac{4.8}{\ln 10} z_A z_B} \approx 10^{-2 z_A z_B}$$

It means that 1 unit increase in the product  $z_A z_B$  is equivalent to a 100-fold decrease in  $A$ .

Let us suppose  $\Delta S_{\text{neutral}}^\ddagger = 0$ , and  $A_{\text{neutral}} = 10^{13} \text{ dm}^3/(\text{mol s})$ , then we have the following data:  
(Left: calculated, right: experimental.)

$z_A$	$z_B$	$A$ $\text{dm}^3/(\text{mol s})$	$\Delta S^\ddagger$ $\text{J}/(\text{mol K})$	$A_{\text{experimental}}$ $\text{dm}^3/(\text{mol s})$	$\Delta S_{\text{experimental}}^\ddagger$ $\text{dm}^3/(\text{mol s})$	Reaction
+3	-1	$10^{19}$	120	$\sim 10^{19}$	$\sim 120$	$\text{Cr}(\text{H}_2\text{O})_6^{3+} + \text{CNS}^-$
+2	-1	$10^{17}$	80	$5 \times 10^{19}$	92	$\text{Co}(\text{NH}_3)_5\text{Br}^{2+} + \text{OH}^-$
0	-2	$10^{13}$	0	$1 \times 10^{14}$	25	$\text{Cr}(\text{H}_2\text{O})_6^{3+} + \text{CNS}^-$
-1	-1	$10^{11}$	-40	$6 \times 10^{10}$	-45	$\text{CH}_2\text{BrCOOCH}_3 + \text{S}_2\text{O}_3^{2-}$
-1	-1	$10^{11}$	-40	$9 \times 10^8$	-71	$\text{ClO}^- + \text{ClO}^{2-}$
-1	-2	$10^9$	-80	$1 \times 10^9$	-80	$\text{CH}_2\text{BrCOO}^- + \text{S}_2\text{O}_3^{2-}$
+2	+2	$10^5$	-160	$1 \times 10^8$	-100	$\text{Co}(\text{NH}_3)_5\text{Br}^{2+} + \text{Hg}^{2+}$
-2	-2	$10^5$	-160	$2 \times 10^4$	-170	$\text{S}_2\text{O}_4^{2-} + \text{S}_2\text{O}_4^{2-}$
-2	-2	$10^5$	-160	$2 \times 10^6$	-130	$\text{S}_2\text{O}_3^{2-} + \text{S}_2\text{O}_3^{2-}$

As it can be seen, experimental determination of the pre-exponential factor can be used to check the reaction mechanism.